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Life Insurance Settlement and Information Asymmetry

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I. Introduction

Life settlement

- ▶ **Life settlement : a transaction which allows policyholders to sell their insurance policies to a investor (settlement provider)**
- ▶ **Alternative Option to surrender**
- ▶ **Surrender value is lower than actuarial value and settlement price is higher than surrender value.**

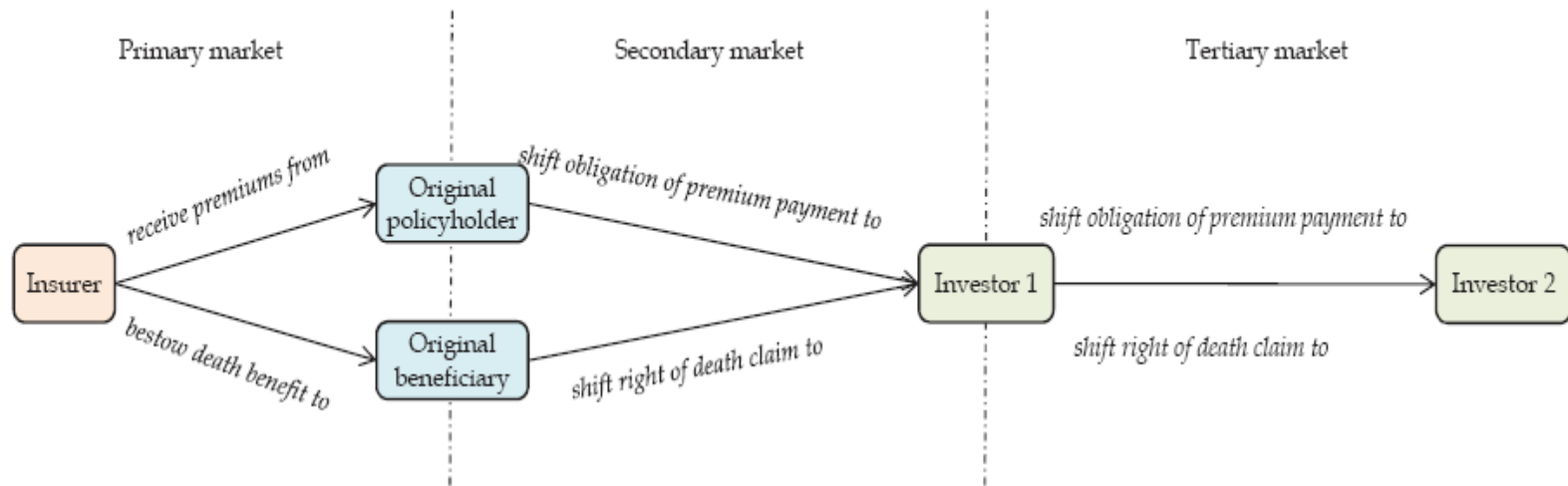
I. Introduction

Life settlement

- ▶ **Illiquid insurance policy(not tradable)→life settlement securitization opens up the secondary market for insurance**
- ▶ **Investors can get an opportunity to invest an asset which is not correlated to their portfolio.**

I. Introduction

Submarket of life insurance



- ▶ **Source: Harvard Business School Background Note 2018–127**

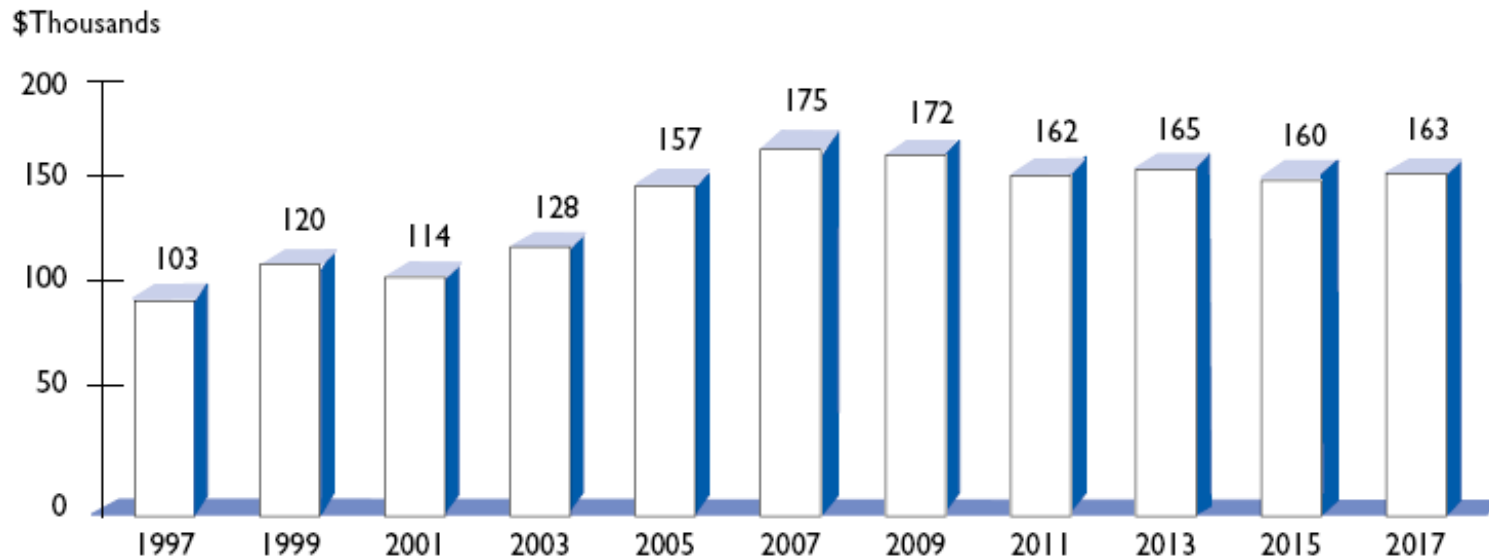
II. Life insurance market overview

- ▶ **Life insurance is owned by 61% of American adults.**
 - **Home ownership :64%**
 - **401 (k) retirement account ownership: 53%**
- ▶ **Of policies (face value)**
 - **60%(31%) of individuals in 2016: whole life & endowment**
 - **40%(69%) of individuals in 2017: term insurance**

II. Life insurance market overview

Life Insurance Market Overview

Average Face Amount of Individual Life Insurance Policies Purchased



자료: American Council of Life Insurers (2018)

II. Life insurance market overview

Life Insurance Market Overview

▶ Termination Rate

	2008	2009	2010	2011	2012
face value	7.6	7.3	6.8	6.1	5.9
# of policy	7.9	6.9	6.1	6.1	5.8

	2013	2014	2015	2016	2017
face value	5.7	5.3	5.4	5.2	5.7
# of policy	5.0	6.2	5.6	6.0	6.4

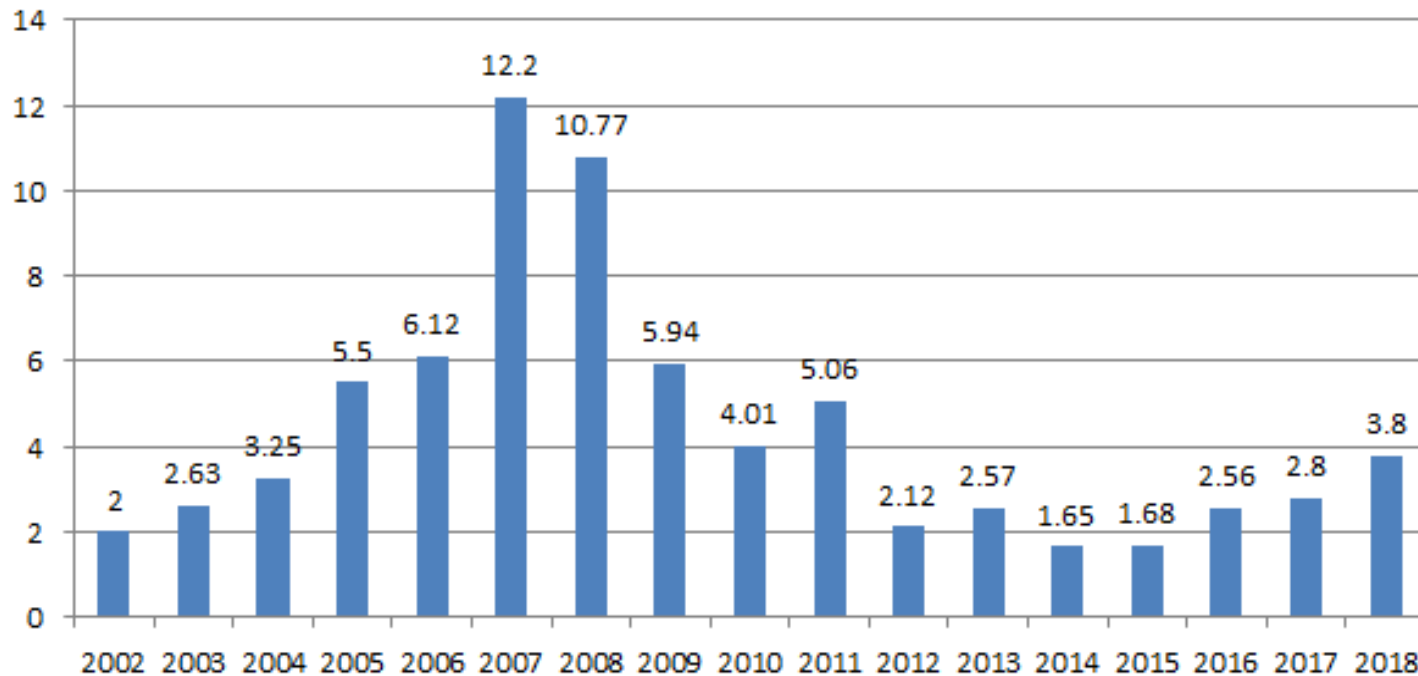
자료: American Council of Life Insurers (2018)

II. Life insurance market overview

- ▶ **Gatzert (2010)**
 - Settlement is allowed in Germany, the U.K. & the U.S.
- ▶ **China Insurance Regulatory Commission (CIRC)**
 - It will run 2-year trial program allowing viatical settlement
- ▶ **The Deal (2015), Magna (2017)**
 - The market size was 1.65 billion dollars (2015)
 - In 2018, the size is projected at 3.4 billion dollars.

III. Life settlement market overview

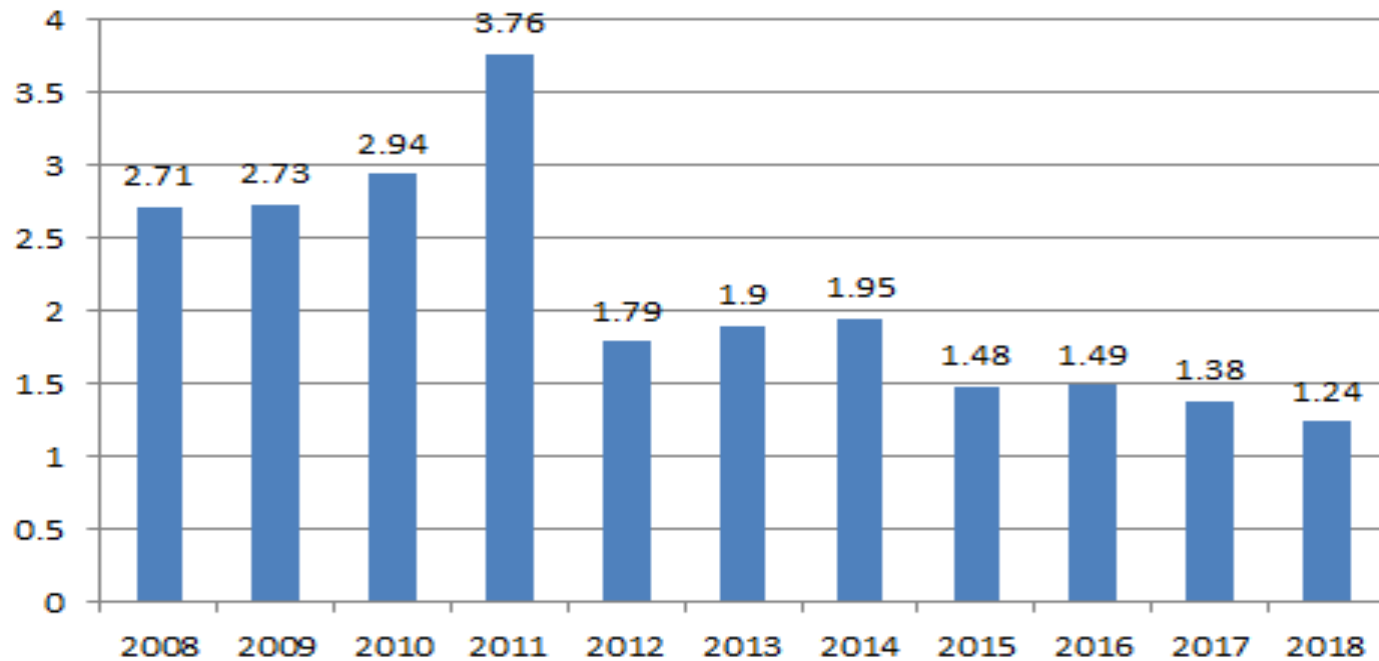
Size of Life settlement market (Face value, billion dollars)



Source: conning (2008), The Deal (2013), Magna report (2018)

III. Life settlement market overview

Size of Life settlement market (Avg Face Value, million dollars)



Source: The Deal (2013), Magna report (2018)

III. Life settlement market overview

Factors For Growths of Life Settlement

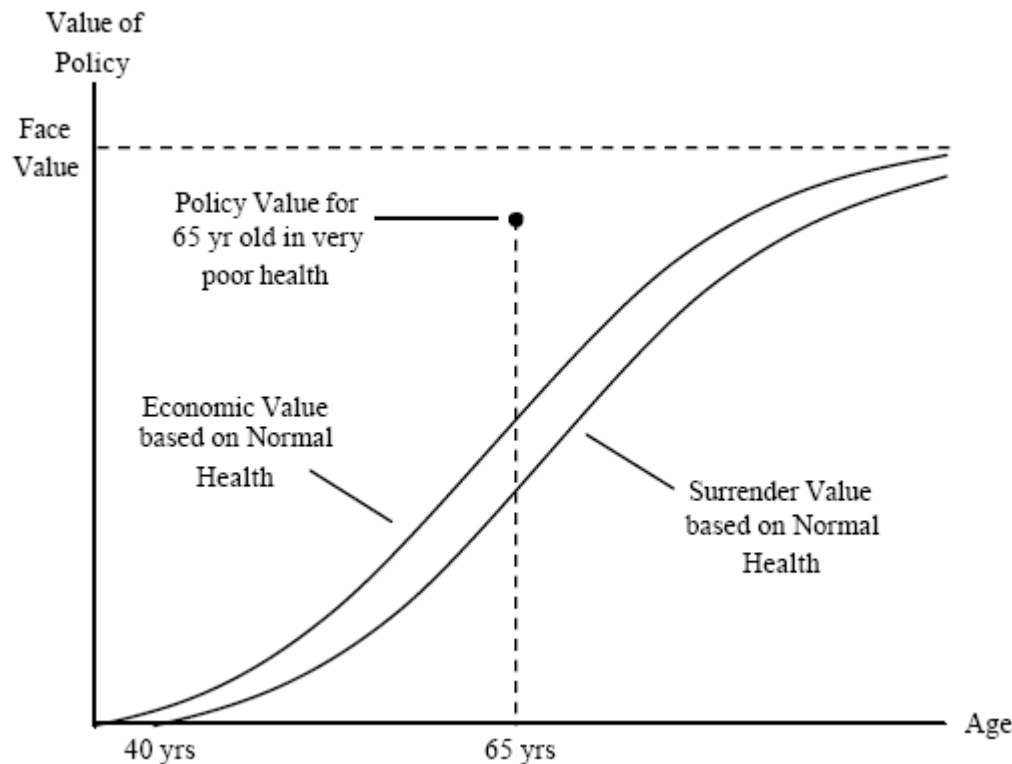
- ▶ **Retirement of Baby boomers**
 - **\$ 143 billion in life insurance owned by people 65 and over was lapsed in 2015.**

- ▶ **Lengthening lifespans**
 - **innovations in medicine & health care**

- ▶ **Increasing accuracy of Medical underwriting**

IV. Literature Review

- **Doherty and Singer (2002)**
 - Settlement market may enhance consumer welfare
 - Reduce the monopsony power of the insurer
 - Loose supported pricing



IV. Literature Review

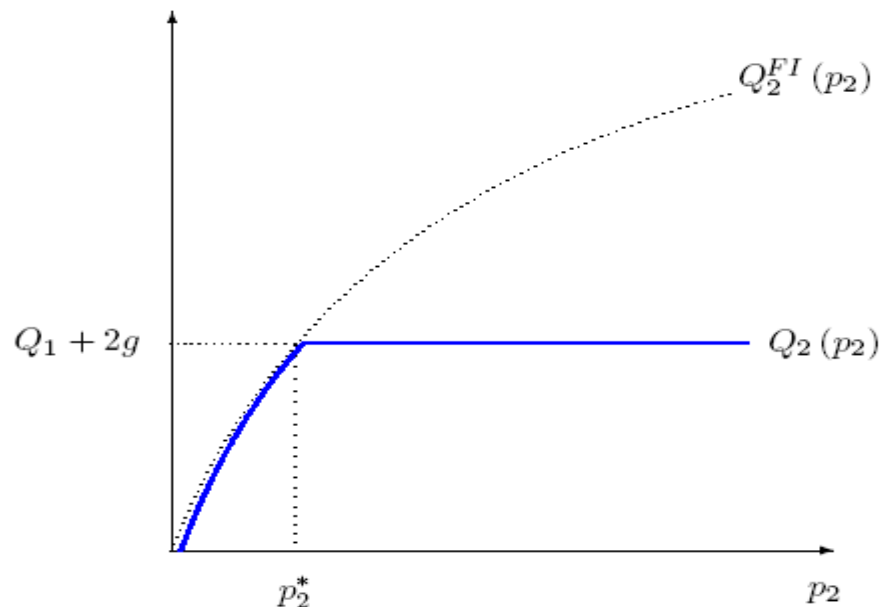
- **Hong and Seog (2018)**
 - Monopolistic insurance market and focusing on the liquidity risk
 - Settlement market may or may not enhance consumer welfare.
- **Seog and Hong (2019)**
 - Monopolistic insurance market and focusing on the liquidity costs of the insurer and policyholders
 - Settlement may help to increase insurance demand and the profit of insurer by saving the liquidity costs.

IV. Literature Review

- **Fang and Wu (2017)**
 - Overconfidence over bequest motives or mortality risks.
 - Settlement market corrects the beliefs and welfare can be improved.
- **Gottlieb and Smetters (2014)**
 - Policyholders exhibit overconfidence over liquidity risks.
 - Settlement market increases consumer welfare, if surrender should occur due to the negative income shock.

IV. Literature Review

- Daily, Hendel and Lizzeri (2008, henceforth DHL), Fang and Kung (2008, henceforth FK)
 - 2-period model in the competitive insurance market
 - “front-loaded” contracts \rightarrow hedge the “reclassification risk”
 - Settlement market lowers consumer welfare since the premium will increase & policyholders cannot hedge the reclassification risk



IV. Literature Review

- **Gatzert et al. (2008)**
 - Settlement market may worsen the insurer's profit by a simulation based on the actuarial assumptions.
 - The profit reduction also leads to the rise of premiums.
- **Braun et al (2012)**
 - Open-end life settlement funds show attractive return as 4.85% of the annualized return. (2003.12~2010.06, AA-Partners dataset) (S&P 500: 0.07%, US Government Bond Index: 0.41%)
 - The volatility is low (2.28%) / Correlation with other asset classes is also low
 - Liquidity, longevity, valuation risk are not captured.
- **Zhu and Bauer (2013)**
 - Realized return of settlement investors is markedly low compared to the expected return(8~12%) due to the information asymmetry regarding mortality risk.
 - The return difference is 5.72%

IV. Motivation

Main Focus

- **Two – dimensional asymmetric information (mortality risk & liquidity risk)**
- **Liquidity risk of policyholders (following HS 2018, HS 2019)**
 - ▶ **Risks to need urgent cash for medical treatment, etc.**
 - ▶ **Policyholders face heterogeneous mortality & liquidity risks & insurers offer menu contract (Q,S)**
 - ▶ **Rothschild and Stiglitz & Wilson condition**

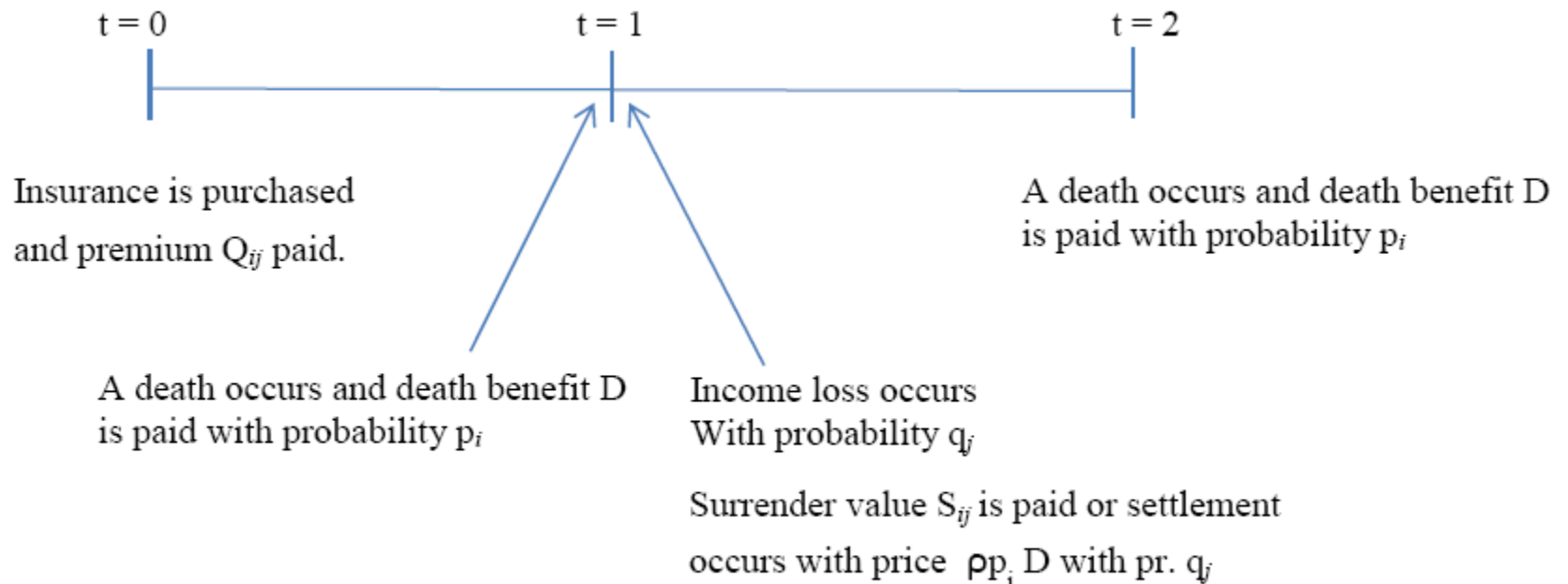
V. Model Description

Assumption

- Competitive insurance market
- 2 sources of risk : Mortality risk i – H,L & liquidity risk j – H, L \rightarrow 4 types of insureds ($ij = HH, HL, LH, LL$)
- 2 periods model: $t = 0, 1, 2$ & Income: W_t or zero
- Discount factor : ρ
- Insured' s utility: u & $u(0)=0$, dependent' s utility: v , $v(0)=0$
- Mortality risk at $t=1$ and $t=2$: p_i
- Income loss y with probability q_j occurs at $t = 1$
- Premium: Q_{ij} & death benefit of insurance : D
- Cash surrender value : S_{ij} , $S_{ij} \leq D$
- Perfect and competitive settlement market, risk neutral investors:
settlement price = $\rho p_i D$
- Contract C_{ij} : (Q_{ij}, S_{ij})
- Expected utility of insured ij given contract C_{ij} : $V_{ij}(C_{ij})$
- The proportion of each risk type : λ_{ij}

V. Model Description

Time Line of Model



VI. The Basic model: benchmark case

- No adverse selection
Without settlement

- Insurance premium for each type.

$$Q_{ij} = \rho p_i D + \rho(1-p_i)q_j S_{ij} + \rho^2 p_i(1-p_i)(1-q_j)D \quad (2.1)$$

- The expected utility of insured ij without settlement :

$$V_{ij}(C_{ij}) = u(W_0 - Q_{ij}) + \rho p_i v(D) + \rho(1-p_i)q_j u(W_1 - y + S_{ij}) + \rho(1-p_i)(1-q_j)u(W_1) \\ + \rho^2 p_i(1-p_i)(1-q_j)v(D) + \rho^2(1-p_i)^2(1-q_j)u(W_2) \quad (2.2)$$

- The slope of the indifference curve on the (Q,S) plane :

$$\frac{dQ_{ij}}{dS_{ij}} = \rho(1-p_i)q_j \frac{u'(W_1 - y + S_{ij})}{u'(W_0 - Q_{ij})} > 0 \quad (2.3)^3$$

- Assumption : $\rho p_H D[1 + \rho(1-q_H)(1-p_H)] - \rho p_L D[1 + \rho(1-q_L)(1-p_L)]$ is positive

VI. The Basic model: benchmark case

- The problem of insurers :

$$\begin{aligned} \underset{Q_{ij}, S_{ij}}{\text{Max}} \quad V_{ij}(C_{ij}) = & u(W_0 - Q_{ij}) + \rho p_i v(D) + \rho(1-p_i)q_j u(W_1 - y + S_{ij}) + \rho(1-p_i)(1-q_j)u(W_1) \\ & + \rho^2 p_i(1-p_i)(1-q_j)v(D) + \rho^2(1-p_i)^2(1-q_j)u(W_2) \end{aligned}$$

$$\text{s.t. } Q_{ij} = \rho p_i D + \rho(1-p_i)q_j S_{ij} + \rho^2 p_i(1-p_i)(1-q_j)D$$

- The FOCs :

$$L_{S_{ij}} = \rho(1-p_i)q_j u'(W_1 - y + S_{ij}) - \lambda_{ij} \rho(1-p_i)q_j = 0 \quad (2.6)$$

$$L_{Q_{ij}} = -u'(W_0 - Q_{ij}) + \lambda_{ij} = 0 \quad (2.7)$$

- Lemma 1. (No adverse selection). Suppose that settlement is not allowed. The optimal insurance contract is satisfied following conditions.

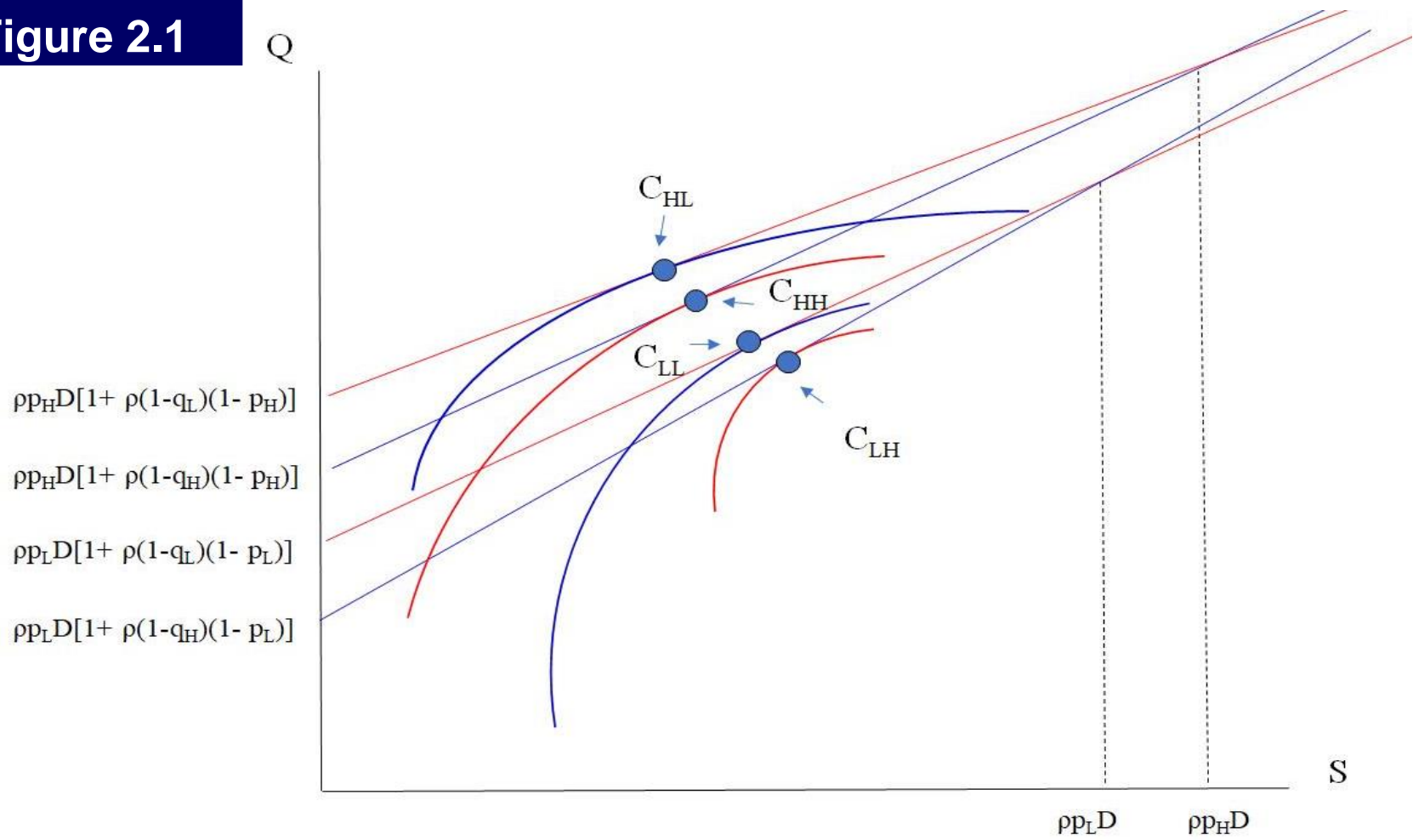
$$(1) \quad u'(W_0 - Q_{ij}) = u'(W_1 - y + S_{ij}), i = H, L, j = H, L$$

$$(2) \quad \text{For } i, (S_{iH} > S_{iL}, Q_{iH} < Q_{iL})$$

$$(3) \quad \text{For } j, (S_{Hj} < S_{Lj}, Q_{Hj} > Q_{Lj})$$

VI. The Basic model: benchmark case

Figure 2.1



VI. The Basic model: settlement is allowed

- No adverse selection
With settlement

- The investors offer the contracts C_H and C_L

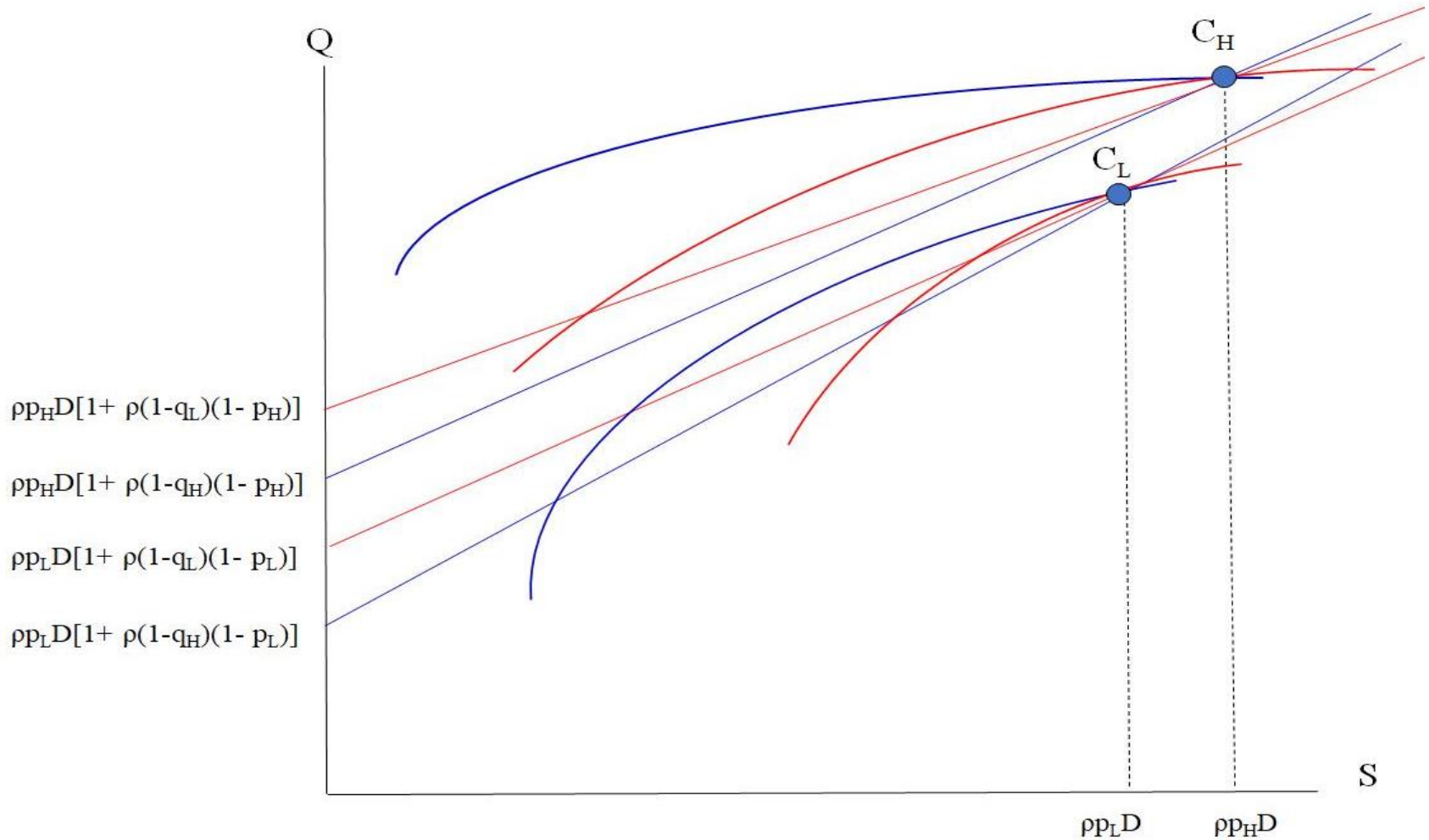
$$(Q_i = \rho p_i D + \rho^2 p_i (1 - p_i) D, S_i = \rho p_i D)$$

- **Lemma 2. (No adverse selection).** Suppose that settlement is allowed. Then the following results hold.

- (1) Optimal contract C_i for ij is $(Q_{ij} = \rho p_i D + \rho^2 p_i (1 - p_i) D, S_{ij} = \rho p_i D)$.
- (2) The utilities of all insureds decrease.

VI. The Basic model: settlement is allowed

Figure 2.2



VII. The model: settlement is not allowed (RS)

- Information Asymmetry

Without settlement

Under RS condition

- The zero profit Pooling line :

$$Q = P + \{ \rho(1 - p_H)[q_H \lambda_{HH} + q_L \lambda_{HL}] + \rho(1 - p_L)[q_H \lambda_{LH} + q_L \lambda_{LL}] \} S$$

Where $P = \rho[(\lambda_{HH} + \lambda_{HL})p_H + (\lambda_{LH} + \lambda_{LL})p_L]D$

$$+ \rho^2 \{ p_H(1 - p_H)[\lambda_{HH}(1 - q_H) + \lambda_{HL}(1 - q_L)] + p_L(1 - p_L)[\lambda_{LH}(1 - q_H) + \lambda_{LL}(1 - q_L)] \} D \quad (3.3)$$

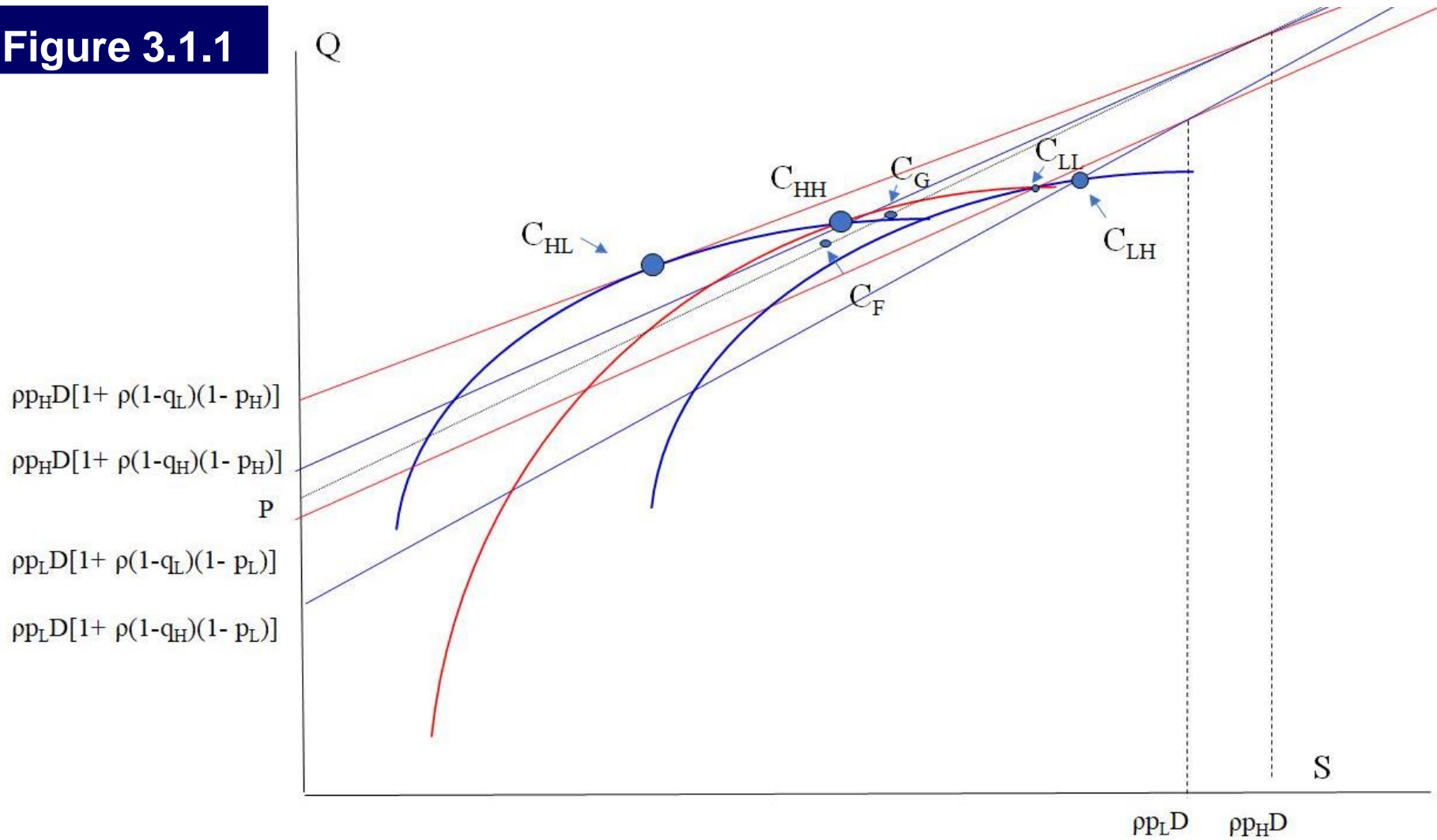
- The zero profit Pooling line for low mortality risks (i = L):

$$Q = \rho p_L k D + \rho(1 - p_L) \frac{\lambda_{LL} q_L + \lambda_{LH} q_H}{\lambda_{LL} + \lambda_{LH}} S \quad \text{Where } k = 1 + \rho \left(1 - \frac{\lambda_{LL} q_L + \lambda_{LH} q_H}{\lambda_{LL} + \lambda_{LH}} \right) (1 - p_L) \quad (3.4)$$

- Separating of Semi-pooling equilibrium

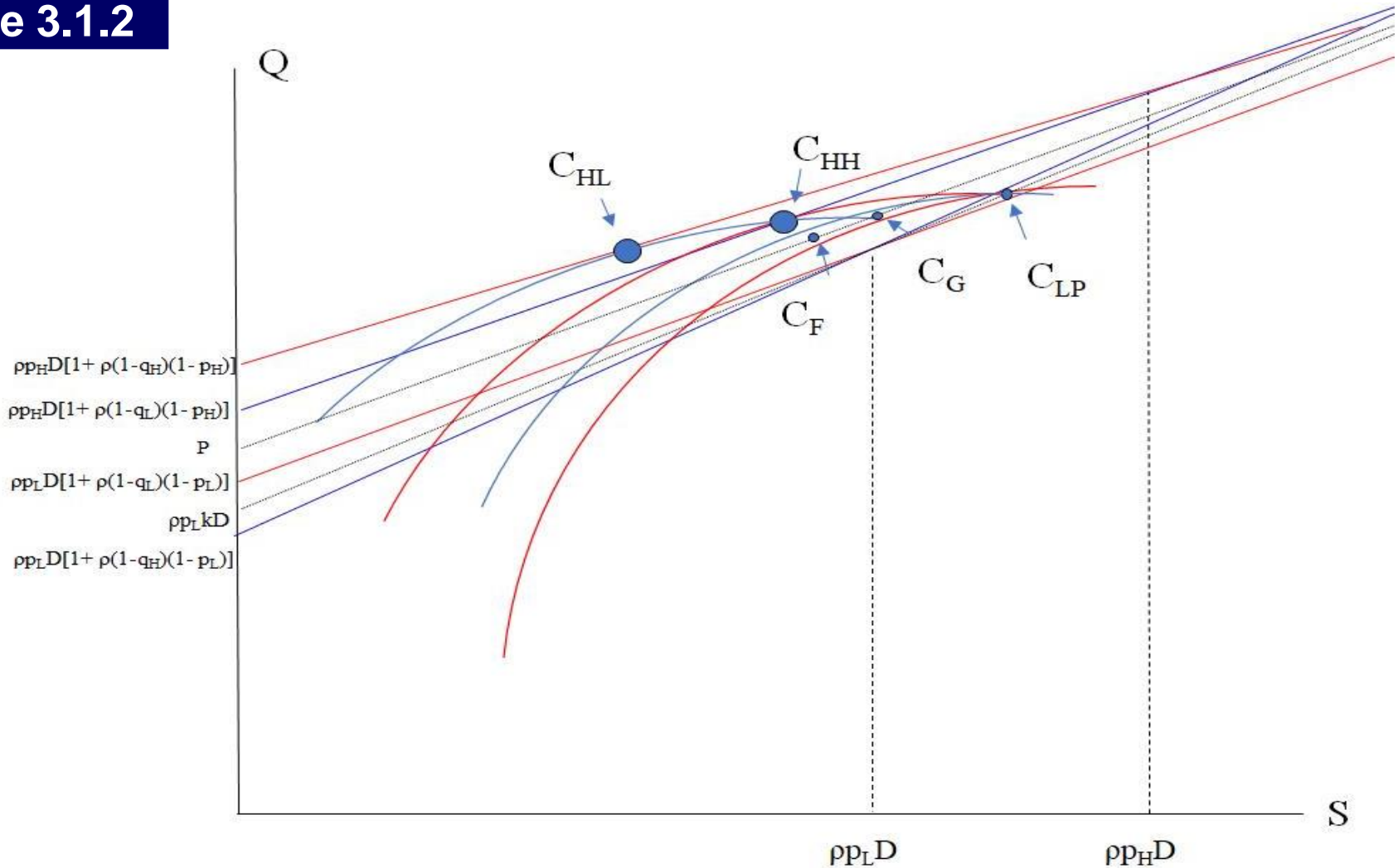
VII. The model: settlement is not allowed (RS)

Figure 3.1.1



VII. The model: settlement is not allowed(RS)

Figure 3.1.2



VII. The model: settlement is not allowed (RS)

- Information Asymmetry

Without settlement

Under RS condition

- **Proposition 1. (Rothschild and Stiglitz) Suppose that settlement is not allowed. Then the following results hold.**

- (1) For HL type, $u'(W_0 - Q_{HL}^*) = u'(W_1 - y + S_{HL}^*)$ while other types ij ,
 $u'(W_0 - Q_{ij}^*) > u'(W_1 - y + S_{ij}^*)$ at the equilibrium.
- (2) The condition for equilibrium depends on the relative proportion of insureds. When equilibrium exists, the condition for RS separating equilibrium is $S < \rho p_L D$, while the condition for semi-pooling equilibrium at which the types with the low mortality risks are pooled while the others are separated is $S \geq \rho p_L D$. S satisfies the following condition (3.2).

$$\begin{aligned}
 & u(W_0 - Q_{HH}^*) + \rho(1 - p_H)q_H u(W_1 - y + S_{HH}^*) \\
 & = u(W_0 - \rho p_L D - \rho(1 - p_L)q_L S - \rho^2 p_L(1 - p_L)(1 - q_L)D) + \rho(1 - p_H)q_H u(W_1 - y + S)
 \end{aligned}$$

Where C_{HH}^* composed of (Q_{HH}^*, S_{HH}^*) is satisfying $V_{HL}(C_{HL}^*) = V_{HL}(C_{HH}^*)$. (3.2)

VII. The model: settlement is allowed (RS)

- Information Asymmetry

With settlement

Under RS condition

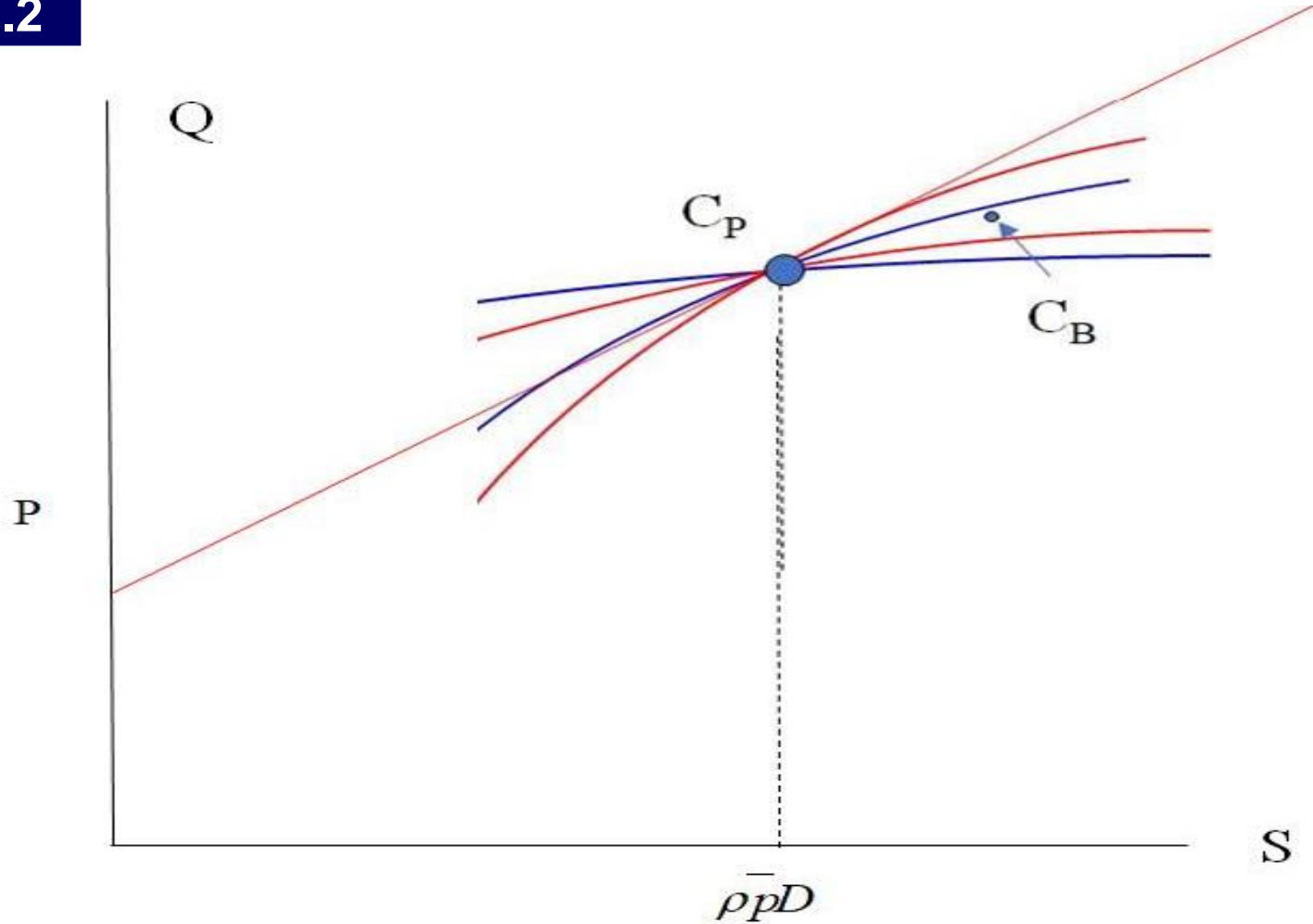
- Insurers cannot offer a pooling contract with $S < \rho \bar{p}D$, where $\bar{p} = \lambda_H p_H + \lambda_L p_L$
Insurers offer $C_p (Q_p, S_p)$ where

$$Q_p = \rho \bar{p}D + \rho^2 D \{ \lambda_H p_H (1 - p_H) + \lambda_L p_L (1 - p_L) \} \\ + \rho^2 D \{ (\bar{p} - p_H)(1 - p_H)[q_H \lambda_{HH} + q_L \lambda_{HL}] + (\bar{p} - p_L)(1 - p_L)[q_H \lambda_{LH} + q_L \lambda_{LL}] \}, S_p = \rho \bar{p}D.$$

→ C_p cannot be an equilibrium.

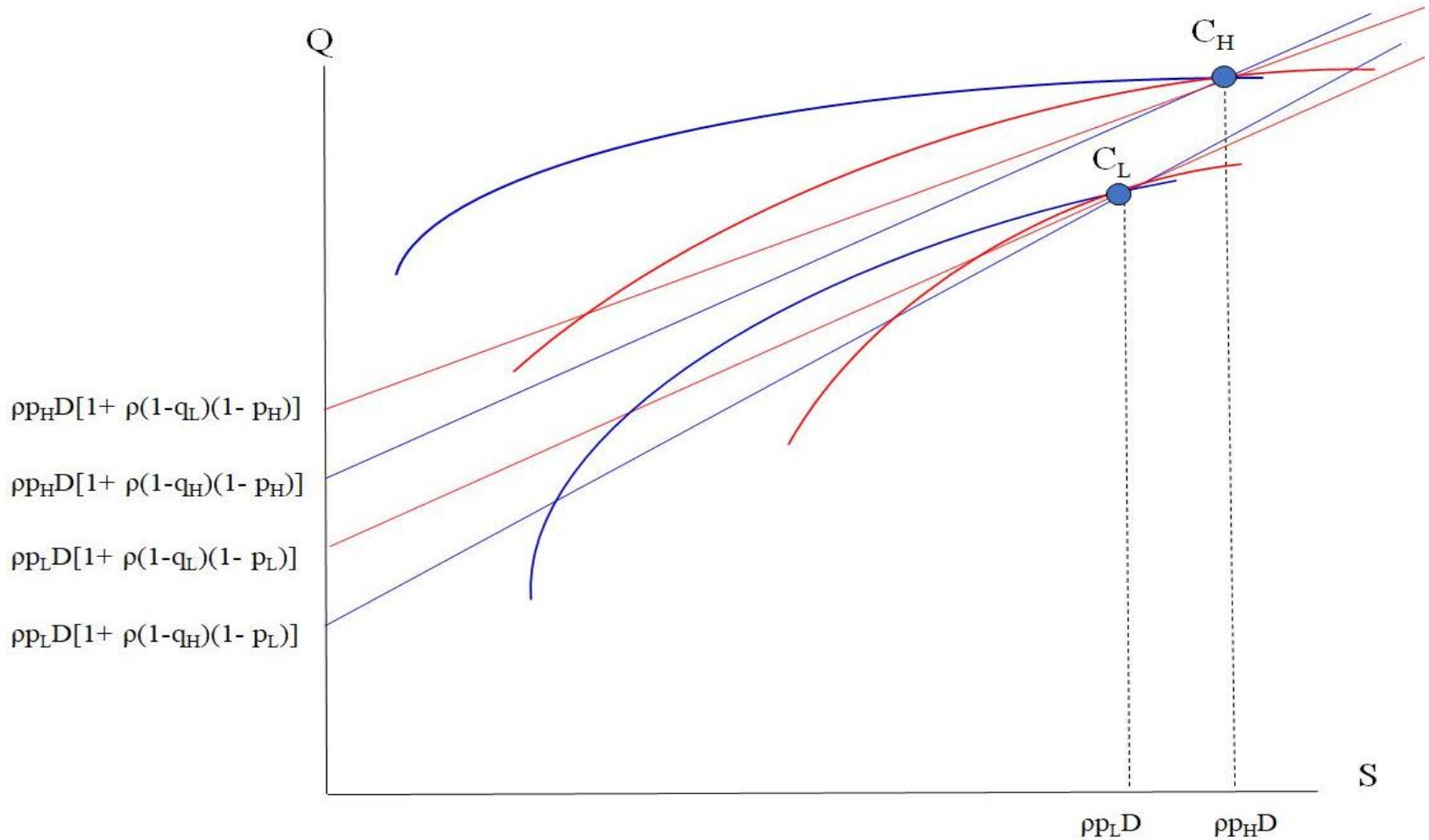
VII. The model: settlement is allowed (RS)

Figure 3.2.2



VII. The Basic model: settlement is allowed

Figure 2.2



VII. The model: settlement is allowed (RS)

- Information Asymmetry
With settlement
Under RS condition
- Insurers may offer a semi-pooling contracts C_{HS} , C_{LS} .
- If the proportion of LH is sufficiently low, then the semi-pooling equilibrium can exist.

Proposition 2. (Rothschild and Stiglitz) Suppose that settlement is allowed. Then the following results hold.

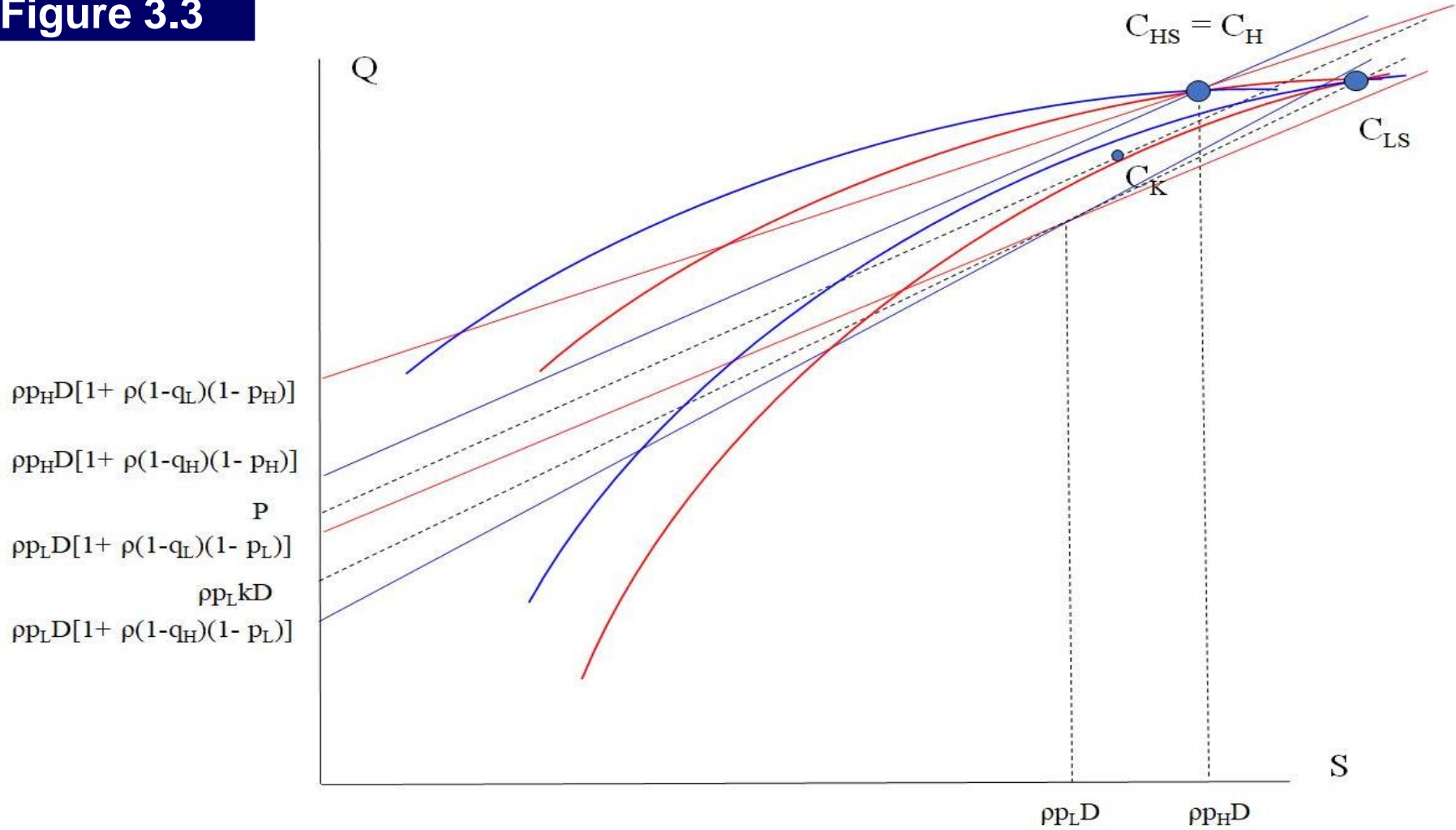
- (1) When equilibrium exists, then the equilibrium is semi pooling at which the same mortality risks are pooled while different mortality risks are separated.
- (2) At the semi-pooling equilibrium, the settlement investors only target the high mortality risks.

Proposition 3. (Rothschild and Stiglitz) Suppose that settlement is allowed. Then the following results hold.

- (1) Insurance premium for all insureds increases.
- (2) The utilities of all insureds decrease.

VII. The model: settlement is allowed (RS)

Figure 3.3



VIII. The model: settlement is not allowed (Wilson)

- Information Asymmetry
Without settlement
Under Wilson condition
- RS separating (or semi-pooling) equilibrium constitutes Wilson equilibrium. Potential Wilson pooling equilibrium is C_{NP}

Proposition 4. (Wilson) Suppose that settlement is not allowed. Then the following results hold.

- (1) If RS separating (or semi-pooling) equilibrium exists, then the equilibrium is Wilson separating (or semi-pooling) equilibrium.
- (2) Pooling equilibrium constitutes Wilson equilibrium. At this equilibrium, following condition holds.

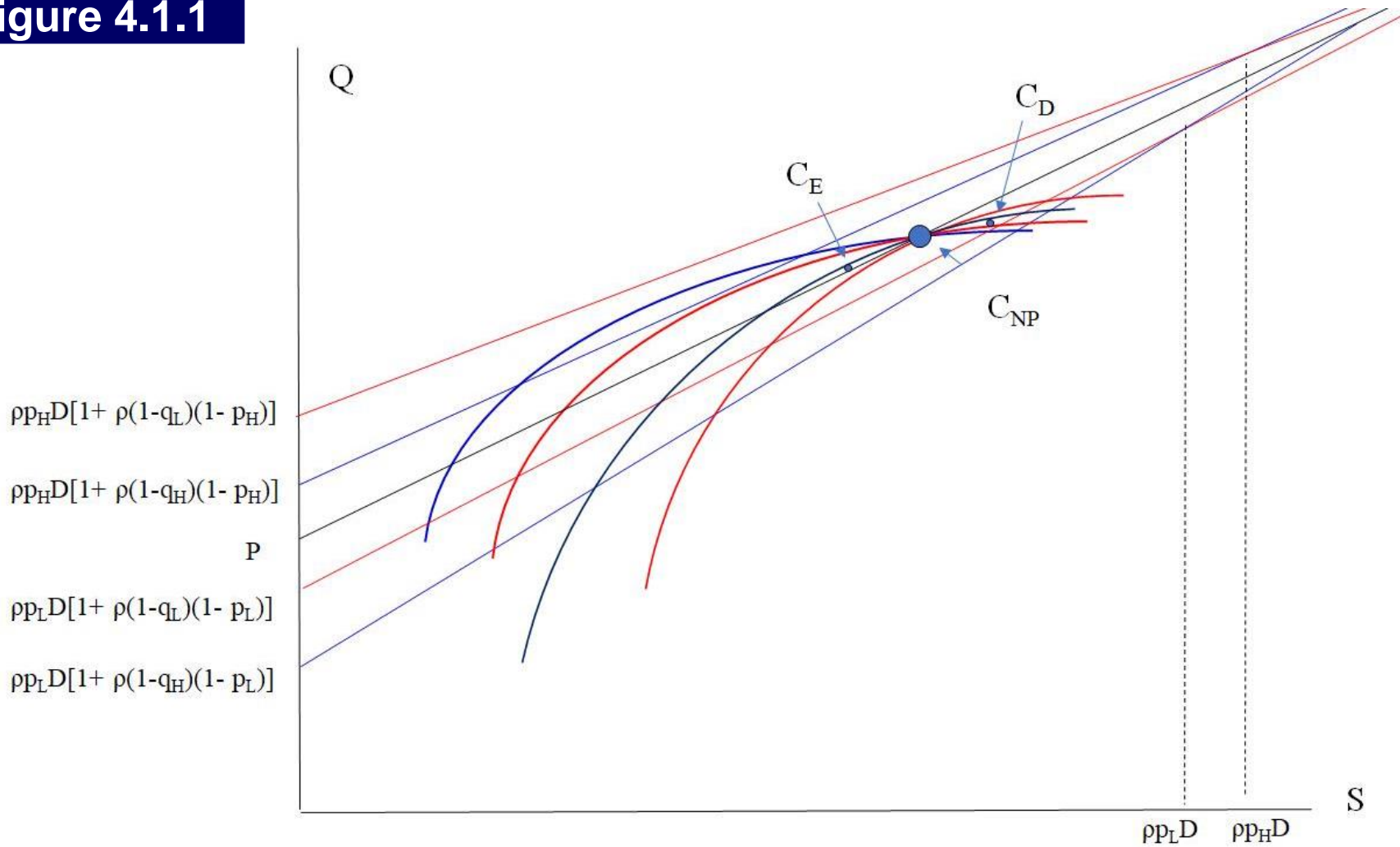
$$(1 - p_H)[q_H \lambda_{HH} + q_L \lambda_{HL}] + (1 - p_L)[q_H \lambda_{LH} + q_L \lambda_{LL}] = (1 - p_L)q_H \frac{u'(W_1 - y + S_{LH})}{u'(W_0 - Q_{LH})} \quad (4.1)$$

- (3) The surrender value at pooling equilibrium is greater than $\rho p_L D$ when the following condition holds.

$$(1 - p_H)[q_H \lambda_{HH} + q_L \lambda_{HL}] + (1 - p_L)[q_H \lambda_{LH} + q_L \lambda_{LL}] < (1 - p_L)q_H \frac{u'(W_1 - y + \rho p_L D)}{u'(W_0 - \rho p_L D - \rho^2(1 - p_L)D)} \quad (4.2)$$

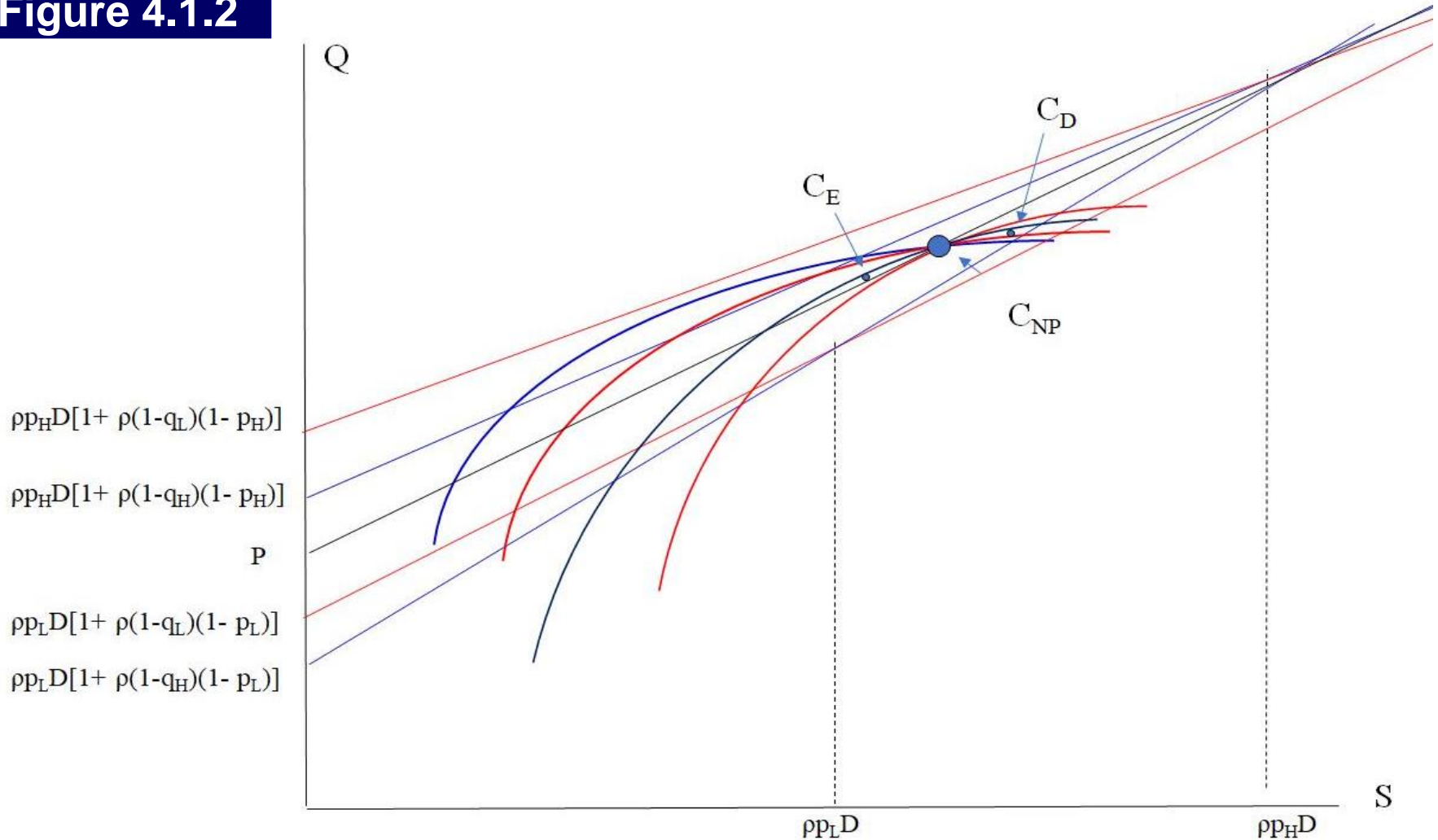
VIII. The model: settlement is not allowed (Wilson)

Figure 4.1.1



VIII. The model: settlement is not allowed (Wilson)

Figure 4.1.2



VIII. The model: settlement is allowed (Wilson)

- Information Asymmetry
With settlement
Under Wilson condition
- RS separating (or semi-pooling) equilibrium constitutes Wilson equilibrium. Potential Wilson pooling equilibrium is C_p
- In figure 3.2.2, if C_B is below the zero profit pooling line, then insurers do not offer C_B

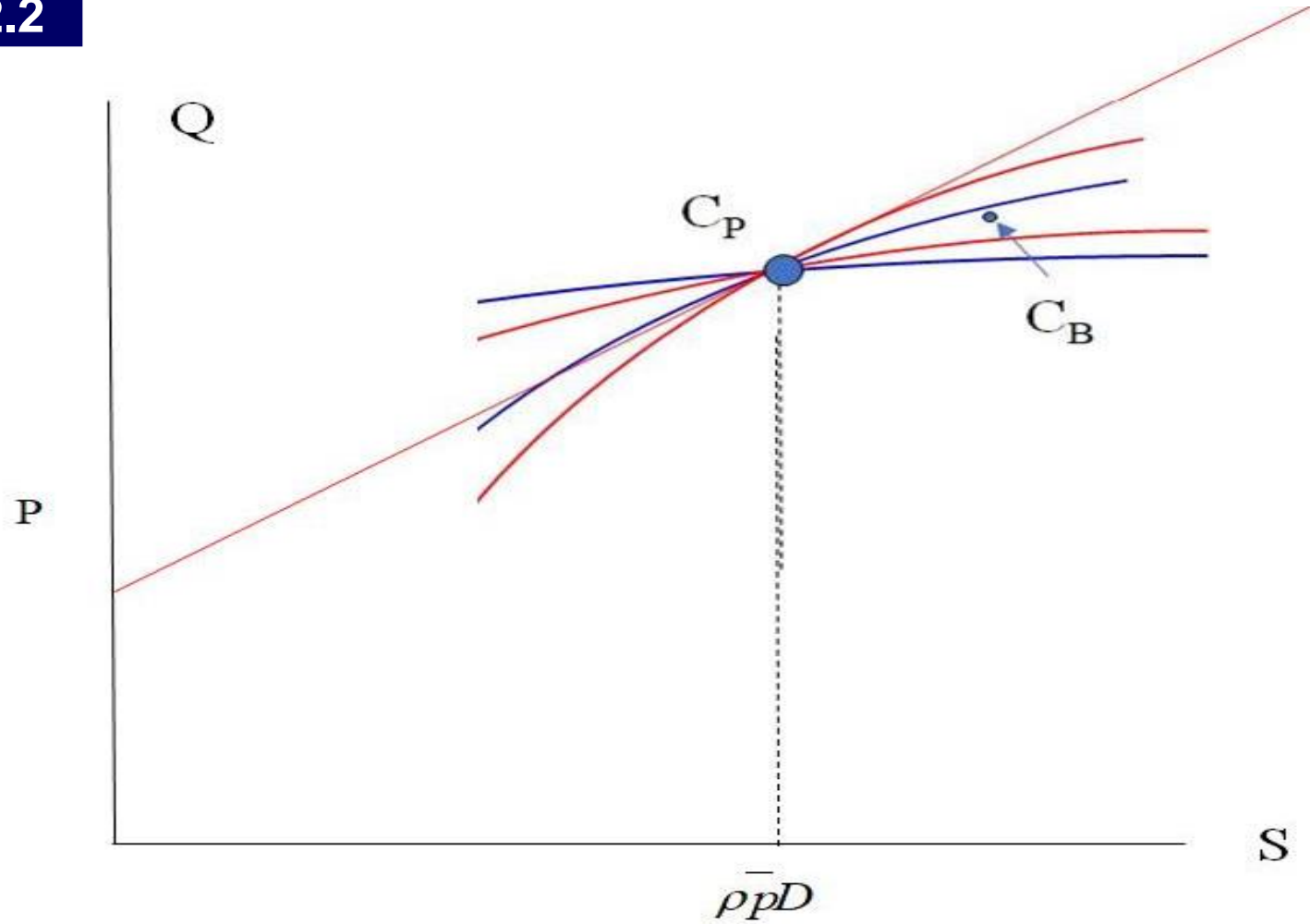
$$(1-p_H)[q_H\lambda_{HH} + q_L\lambda_{HL}] + (1-p_L)[q_H\lambda_{LH} + q_L\lambda_{LL}] \geq (1-p_L)q_H \frac{u'(W_1 - y + \rho\bar{p}D)}{u'(W_0 - Q_p)}$$

where $Q_p = \rho\bar{p}D + \rho^2D\{\lambda_H p_H(1-p_H) + \lambda_L p_L(1-p_L)\}$
 $+ \rho^2D\{(\bar{p} - p_H)(1-p_H)[q_H\lambda_{HH} + q_L\lambda_{HL}] + (\bar{p} - p_L)(1-p_L)[q_H\lambda_{LH} + q_L\lambda_{LL}]\}$ (4.3)

- The expected utility of LH may or may not be maximized at C_p

VIII. The model: settlement is allowed (RS)

Figure 3.2.2



VIII. The model: settlement is allowed (Wilson)

Proposition 5. (Wilson) Suppose that settlement is allowed. Then the following results hold.

- (1) If (4.3) hold, RS semi-pooling contract with settlement or pooling contract can be Wilson equilibrium contract. The pooling contract is C_P denoted as $(Q_P, \rho \bar{p}D)$ where

$$Q_P = \rho \bar{p}D + \rho^2 D \{ \lambda_H p_H (1 - p_H) + \lambda_L p_L (1 - p_L) \} \\ + \rho^2 D \{ (\bar{p} - p_H)(1 - p_H)[q_H \lambda_{HH} + q_L \lambda_{HL}] + (\bar{p} - p_L)(1 - p_L)[q_H \lambda_{LH} + q_L \lambda_{LL}] \}$$

- (2) If (4.3) does not hold, the following cases hold.
- If the equilibrium contract without settlement is RS separating (or semi-pooling), then the RS semi-pooling contract with settlement or pooling contract C_P can be an equilibrium.
 - If the equilibrium contract without settlement is pooling contract, then the equilibrium contract does not change.
- (3) Settlement market does not exist when the following conditions hold.
- (4.3) does not hold and the equilibrium contracts with and without settlement are separating (or semi-pooling) and pooling, respectively.
 - (4.3) does not hold and the equilibrium contract without settlement is pooling.

VIII. The model: settlement is allowed (Wilson)

Proposition 6. (Wilson) The effects of settlement are as follows.

- (1) Insurance premium for some insureds may increase. There exists the case in which the premium for all insureds decrease.
- (2) The utilities of some insureds may increase. There does not exist the case in which the utilities for all insureds increase.

VII. Conclusions

⟨Under RS condition⟩

- **Without settlement , risk types are fully separated or semi-pooled where liquidity risks with low mortality risk are pooled if an equilibrium exists.**
- **With settlement, a semi-pooling equilibrium may exist in which liquidity risks are pooled while mortality risks are separated.**
- **The utilities of all insureds decrease.**

⟨Under Wilson condition⟩

- **Without settlement ,a pooling equilibrium exists.**
- **With settlement, a pooling equilibrium may exist.**
- **There exists the case that settlement market does not exist.**
- **The utilities of some insureds may increase.**

Thank you!